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POSITION DETERMINATION WITH LORAN-C TRIPLETS AND THE HEWLETT-PACKARD HP-67/97 PROGRAMMABLE CALCULATORS

by

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Naval Postgraduate School Monterey, California

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March 1980

The programs in this report are for use within the Navy, and they are presented without representation or warranty of any kind.

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ABSTRACT

This report presents an algorithm and HP-67/97 programs for position determination with Loran-C chains. Operational data cards are prepared in advance for Loran-C triplets. Position determination is performed using a single program card and an appropriate operational data card.

A. Introduction

The Loran system is a radio aid to navigation which utilizes the principle of hyperbolic fixing. The locus of points for which the difference in arrival time of synchronized signals from a pair of transmitters is constant determines a hyperbolic line of positions (LOP). The intersection of two hyperbolic lines of position from two pairs of transmitters determines position or a hyperbolic fix. That two pairs of stations are required for a fix does not necessarily mean that there are four separate stations, for one station of one pair may be colocated with one station of the other pair forming a *Loran triplet* (Figure 1). Triplets may be joined "end-to-end" by station colocation to form a *Loran chain* (Figure 2). Loran chains are common on both the East and West Coasts of the North American continent.

The early "Standard Loran" or Loran-A" operating at a frequency just below 2MHz is still in use in the Pacific area. The present day "Loran-C" operates at 100-kHz and is in use in both the Atlantic and Pacific Areas. The computational algorithm and programs described herein can be used for position determination with Loran-C triplets. Further information on the history, development and operation of the Loran systems may be found in References 1 and 2.







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B. Program Description

One program card and one operational data card (described below) are all that is required for on-location position determination from Loran triplet time-difference measurements. Two program cards are required to prepare operational data cards; these operational data cards should be prepared and validated prior to on-location navigational use. Thus although three program cards are described only one program card is required for navigation; two program cards are used to prepare operational data cards during or prior to mission planning. The function of each program card and its intended use follows.

<u>Program Card 1</u>. This program card is used to prepare master data cards. A master data card requires the following information for a master(M) station/slave(S) station pair:

- 1. A M/S pair identification number.
- The quantity At which is the sum of the coding delay plus the one way base line time in microseconds.
- 3. The latitude and longitude of the master station.
- 4. The latitude and longitude of the slave station.

Some preprocessing of these data is performed before the master data card is generated. The data generated require only one side of an HP-67/97 magnetic card for each M/S pair, thus a second M/S pair may be placed on side 2 of the card (thus conserving cards) if desired. It is envisaged that a master data card will be prepared in advance for each M/S pair that might be received within an area of operation.

<u>Program Card 2</u>. This program card is used to prepare an operational data card for every Loran triplet within an operational area. Each operational data card contains data merged from the master data cards which contain M/S pair information for each pair of the triplet. These merged data are validity checked, colocation of master or slave determined and encoded.

The only inputs required for this program are the two master data cards that comprise the Loran triplet. It is possible to prepare and store operational data cards rather than master data cards. This may be desirable if there is no scarcity of cards and storage space, however the number of possible Loran triplets is considerably larger than the number of M/S pairs.

Program Card 3. This program card is used in conjunction with an operational data card for position determination. Required input is the indicated time difference T for each M/S pair of the triplet. Output is the computed latitude and longitude of the fix. Note: Every Loran fix has two possible solutions. The unwanted solution can almost always be rejected by inspection, however, if the stations of the Loran triplet are nearly aligned then either solution may be valid even though only one solution should be consistent with the flight plan.

C. <u>HP-67/97</u> Calculator Programs

1. User Instructions

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Step	Instructions	Input Data/Units	Keys	Output Data/Units
1.	Read in program card (both sides)			
2.	Input a unique ID number for the Loran pair*	ID	fa	ID
3.	Input the coding delay Δt	Δt	fc	Δt
4a. b.	Input the master station latitude and longitude (CHS for West)**	^ф м ^λ м	↑ A	
5a. b.	Input the slave station latitude and longitude (CHS for West)	∲s ^λ s	† C	
6a. b.	Run Pass a blank data card through the card reader.	None	Е	crd
* Note: Loran pairs are coded on the navigation maps using designators such as 9930X, 9930Y, 9930Z and 9930W. It is suggested that the ID's for these pairs be coded as 9930.1, 9930.2, 9930.3 and 9930.4, respectively. However, any consistent scheme is acceptable.				
	<pre>** The format for position data inpu _+DDD.MMSSFF, where</pre>	t is of the	form:	
	DDD denotes degrees MMM denotes minutes SS denotes seconds FF dnotes hundredths of	a second.		

CARD 1

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and in many atta

The minus sign (-) denotes Southern latitudes or Western

Step	Instructions	Input Data/Units	Keys	Output Data/Units
1.	Read in program card 2			
2a.	Start		Е	9.00
b.	9.00 will flash in the display. Insert a master data card containing the first pair of a Loran triplet.			
c.	9.00 will flash in the display once more. Insert a master data card containing the second pair of the Loran triplet.			9.00
d.	If the data form a proper triplet, "crd" will appear in the display.			crd
e.	Pass both sides of a blank card thru the card reader to produce the operational data card for the Loran triplet.			
	Should "error" appear in the disp cards do not compare to form a Lo and longitude of the colocated st both master data cards in order t operational data card.	play, then the pran triplet. cations must b co successfull	two mas Both th e identi y produc	ster data ne latitude .cal on :e an
	Label the A key position with the <u>first</u> Loran pair (the pair insert key position with the identificat pair (from Step 2c).	e identificati ed in Step 2b ion number of	on numbe) and la the sec	er of the abel the B cond Loran

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CARD 3	3
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Step	Instructions	Input Data/Units	Кеуб	Output Data/Units
1.	Read in both sides of the program card 3.			
2.	Read both sides of the operational data card for the Loran triplet that you are receiving.			
3a.	Set to compute Solution A.		fa	
b.	Set to compute Solution B.		fb	
4.	Input the observed time delay from the first Loran pair.	т	A	
5.	Input the observed time delay from the second Loran pair.	Т	В	
6.	Compute fix Latitude Longitude		E R/S	Latitude Longitude
7.	Repeat from Step 2 with a new operational data card or from Steps 3 or 4 as required.			

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2. Sample Problem

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CARD	1
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Step	Instructions	Input Data/Units	Keys	Output Data/Units
	In this series of examples we will prepare and use data cards for the Loran-C pairs 9930X and 9930Y.			
1.	Read in program card l (both sides)			
2.	Input the ID for 9930X	9930.1	fa	9930.10
3.	Input the coding delay Δt for 9930X	36389.66	fc	36389.66
4a. b.	Input the master station latitude and longitude (CHS for West)	34.034604 -77.544676	† A	
5a. b.	Input the slave station latitude and longitude (CHS for West)	46.463218 -53.102816	† C	
6a. b.	Compute Pass a blank data card through the card reader. Label the card 9930X MASTER	None	Е	crd
7.	Input the ID for 9930Y	9930.2	fa	9930.2
8.	Input the coding delay Δt for 9930Y	52541.31	fc	52541.31
9a. b.	Input the master station latitude and longitude (CHS for West)	34.034604 -77.544676	↑ A	
10a. b.	Input the slave station latitude and longitude (CHS for West)	41.151193 -69.583909	t C	
11a. b.	Compute Pass a blank data card (or the second side of the card used in Step 6b) through the card reader. Label the side 9930Y MASTER	None	Е	crd
12.	These two cards will be used in the next example.			

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CARD	2
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Step	Instructions	Input Data/Units	Keys	Output Data/Units
1.	Read in program card 2.			
2a.	Start		Е	9.00
þ.	While 9.00 is flashing in the display, insert the MASTER data card for station 9930X into the card reader.			
с.	When 9.00 starts flashing in the display again, insert the MASTER data card for station 9930Y into the card reader.			9.00
d.	"Crd' will appear in the display.			crd
e.	Pass both sides of a blank card through the card reader. Label this card 9930X/9930Y OPERATIONAL DATA CARD. Then label the A key position 9990X and the B key position 9930Y. This card will be used in the next example.			0.00

and the second

CARD	3
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Step	Instructions	Input Data/Units	Keys	Output Data/Units
	You are receiving 9930X and 9930Y and wish to obtain a fix.			
1.	Read in program card 3 (both sides)			
2.	Read in the operational data card for the triplet 9930X/9930Y (both sides)			
3.	Select Solution A.		fa	
4.	The indicated time delay is 49400 µs from 9930Y. Input the indicated time delay.	49400	в	0.00
5.	The indicated time delay is 28800 μ s from 9930X. Input the indicated time delay.	28800	A	0.00
6.	Solution A: 42°44'57"N Latitude 41°07'32"W Longitude Solution B: 27°00'07"S Latitude 102°27'12"E Longitude Since you are navigating over the North Atlantic, Solution A is the desired fix.		e R/S	42.4457 -41.0732
7.	Repeat from Step 2 with a new operational data card or from Steps 3 or 4 as required.			

a cust

	Card 1.				
Regi	sters:				
R0:	ID	S0:	L	RA:	
Rl:	Δt	S1:	т	RB:	
R2:	2c	S2:	U	RC:	θ _m
R3:		S3:	v	RD:	∆0m
R4:	θ _M	S4:	x	RE:	Δλ
R5:	λ _M	S5:	Y	RI:	Δλ
R6:	[£] мs	S6:	δlq		
R7:	^θ s	S7:	$\Delta \lambda_{\mathbf{m}}^{*}$		
R8:	$^{\lambda}$ s	S8:	d		
R9:	^ξ sm	S9:	f		

3. Program Storage Allocations and Program Listings

Initial Flag Status and Use:

0:	OFF,	Unused	2:	OFF,	Unused
1:	OFF,	Unused	3:	OFF,	Unused

Display Status:

DSP 4, FIX, DEG.

User Control Keys:

Α:	$\Phi_{\mathbf{M}} \stackrel{\uparrow}{\longrightarrow} \lambda_{\mathbf{M}}$	a:	Station	ID
B:		b:		
С:	${}^{\phi}\mathbf{S} \stackrel{\dagger}{} {}^{\lambda}\mathbf{S}$	c:	Δt	
D:		d:		
E:	Prepare data card	e:		
		12		

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	Card 2.				
<u>Regi</u>	sters:				
R0:	\pm ID ₁	S0:	\pm ^{ID} ₂	RA:	
Rl:	Δt ₁	S1:	∆t ₂	RB:	
R2:	2c ₁	S2:	^{2c} 2	RC:	
R3:		S3:		RD:	
R4:	θAl	S4:	^θ A2	RE:	a _p = 21295.87
R5:	λ _{Al}	S5:	λ_{A2}	RI:	f = 1/298.26
R6:	ζAl	S6:	^ξ a2		
R7:	θΒ1	S7:	^θ B2		
R8:	λ _{Bl}	S8:	^λ B2		
R9:	^ξ B1	S9:	^ξ в2		

Initial Flag Status and Use:

0:	OFF,	Vertex determination	2:	OFF,	Validity	checking
1:	OFF,	Unused	3:	OFF,	Unused	

Display Status:

DSP 2, FIX, DEG

User Control Keys:

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Α:		a:
B:		b:
C:		с:
D:		d:
E:	Run	e:

13

	Card 3.				
Regi	sters:				
R0:	ID ₁	S0:	ID ₂	RA:	М
Rl:	Δt _l	Sl:	∆t ₂	RB:	u, N
R2:	(2c) ₁	S2:	(2c) ₂	RC:	D, d
R3:	A ₁ , c ₂ , P	S3:	^A 2	RD:	Δσ
R4:	$\theta_1 = \theta_F$	S4:	^θ 2	RE:	a _p = 21295.87
R5:	$\lambda_1 = \lambda_F$	S5:	^λ 2	RF:	f = 1/298.26
R6:	٤	S6:	^ξ 2		
R7:	с ₁ , с ₁ , н	S7:	с ₂		
R8:	B_1 , S/a = r	S8:	^B 2		
R9:	α ₁	S9:			

Initial Flag Status and Use:

0:	OFF,	Soln A, Soln	В	2:	OFF,	M/S Vertex Flag
1:	OFF,	Unused		3:	off,	Unused

Display Status:

DSP 2, FIX, DEG

User Control Keys:

Α:	T ₁	a:	Soln	Α
B:	T ₂	b:	Soln	В
C:		c:		
D:		d:		
Е:	Run	e:		

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Main Routine: Renewal Solution Compute and/or	store:		$\theta_{\rm m} = (\theta_1 + \theta_2)/2$	7 T W					Δθ = (θ ₂ -θ ₁)/2				$\Delta \lambda = \lambda_{-} - \lambda_{-}$			$\Delta \lambda = \Delta \lambda / 2$				$H = \cos^2 \Delta \theta \sin^2 \theta$												2	$I = sin \Delta \theta + H sin \Delta \theta$		
21 15 36 84 36 84	រដូន ន	-24	35 13	36 07	36 84	-40	20	-24	35 14	36 62	36 85	140	35 15	29 9	- 1-	35 46	16-51	36 14	42	15 15	36 13	41	5	1077 -	36 46	41	20	50 -	36 14	11	in No	-55	35 60	-21	ta Card
#LBLE RCL4 RCL7	i + '	۱۰	ST0C	RCL7	RCL4	ı	2	.1.	ST0D	RCL8	ROL5	•	STOE	N	.1.	1012	P#S	RCLD	503	Χŝ	RCLC	SIH	ы Х	ı	RCLI	SIN	ei X		RCLD	NIS	сх Х	+	ST08	ENT 1	er Dat
039 049 041		643 643	845	846	647	648	049	020	651	052	653	054	055	056	667	658	620	669	861	230	693	064	665	066	667	. 065	669	619	ê71	672	873	674	075	076	Mast
Store Station ID.	Ctores At		Store longitude		and store parametric latitude	of the master station.				Store longitude and	store barametric latitude	score har anner transcare	of the slave station.				Subroutine to		convert	geographic (geodetic)	1-+:+::30 +0		parametric latitude.						Store flattening	constant.					Card 1: Prepare
11 91 12 11 91 12	21 16 17	1 2 2 2	11 12	16 36	35 85	23 02				16 36		23 63	35 87	ч сц	21 03	1+-	16 35	1:j *#	61		5	ŝ	29	-63	30	5 F.	(4) - 145 1	16-51	35 62	16-51	- 45	- 35	16 43	24	
#LFL0 . 5700 57N	#LELO	NLa	#TELH	* 10 Li H	5105	5-1-1-5 5-1-1-5 5-1-1-5	5104	E TN	¢LELC	H100+	5105	6369	S707	FTN	*LEL9		HM3+	TÁN		ENTI	N 1	QU	S	•	r 4 1	: م	× ;	54	5109	P=S	ı		-NHT	RTN	
199 199 199	664	1999 1999	E E	603	690	01 ē	e	210	613	614	ele	016	617	616	019	070	8 <u>5</u> 1	625	929	6) 6			627	6	630	929	631	632	10) 10) 10)	634	635	636	637	038	

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Y = U = Y	$\delta_{\mathbf{I}} \mathbf{d} = \mathbf{f}(\mathbf{T}\mathbf{X} - \mathbf{Y})/4$	$2c = S/a_e = (T-\delta_1 d) \sin d$	F/2 = [Y - (1-2L) (4-X)] -2G = fT
88 8 88 88480228	6 6 8 8 8 6 8 8 4 6 9 6 8 4 6 9 6 9 7 4 6 9 6 9 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	39999999999999999999999999999999999999	86 8 86 8 87 81 81 81 81 81 81 81 81 81 81 81 81 81
FCL2 FCL3 5705 CHS FCL4 FCL4	+ 8106 8106 8106 818 818 818	ENCLES F118 F118 F118 F118 F118 F118 F118 F11	RCL9
		5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	444444866644 44446666 8446666 8446666 8446666 8446666 846666 846666 846666 846666 846666 846666 84666 84666 84666 84666 84666 84666 84666 84666 84666 84666 84666 84666 84666 84666 846 84
d = cos ⁻¹ (1-2L)	T = d/sin d	$u = 2 \sin^2 \theta_m \cos^2 \ell \theta_m / (1-L)$	$\mathbf{v} = 2 \sin^2 \Delta \theta_m \cos^2 \theta_m / \mathbf{L}$ $\mathbf{x} = \mathbf{U} + \mathbf{V}$
58.69 69.69	198 8 19292349090		8 88 8 3898678868
	510 510 510 510 510 510 70 70 70 70 70 70 70 70 70 70 70 70 70	RCL0 8702 8702 8702 8702 8718 8718 8718 8718 8718 8718 8718 871	ENTT ENTT ENTT ENTT FCL0 FCL0 FCL2 FCL2 ST04
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store ^α 12 in R ₆ and ^α 21 in R ₉ .				
88 88 88 88 88 88 88 88 88 88 88 88 88				
5155 5165 5165 5165 5175 8 7165 8 7165 8 777 777 8 777 8 777 8 777 8 7777				ed.
111111111111 1111111111111 11111111111				ntinu
-FG 2 = -(FG tan Δλ)/4	Δλ' = (Δλ + Q)/2	cosΔθ cosΔλ" sin θ sinΔλ" t ₂ is in the Y-register	- $\sin \Delta \theta_m \cos \Delta \lambda_m^{'}$ cos $\theta_m \sin \Delta \lambda_m^{'}$	t _l is in the X-register Card 1: Co
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						1/f				store two required constants and	write Operational	Card Data.			Subroutine	Wait for a Master	Data Card to be read,	then merge and	return.		Subroutine	Determine if the	bair master stations	or slave locations	are colocated.			~	Set F2 if a colocation	is found.			
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Card 2: Prepare Operational Data Card.

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delay input is not valid Error at Step 75 if time for one of the pairs. $= B_2 A_1 - B_1 A_2$ Fixing Routine ξ2 $B_2C_1 \sin \xi_1$ 5 $B_1C_2 \sin \xi_2$ ഗ cos cos ≻ and and $_{B_1C_2}^{B_1C_2}$ $^{B}2^{C}_{1}$ υ ¥ q 1989.78 21 888.88 48 48 8 288.78 289.499.497.886.486.447.886.447.447.886.447.886.447.886.447.886.447.886.447.447.886.447.447.886.447.447 であ 11 - 35 23 65 29 65 29 65 16 Loran Fixing Program **6.014.010 6.014.0100 6.014.0100 6.014.0100 6.014.0100 6.014.0100 6.014.0100 6.014.01000 6.014.01000 6.014.010000 6.014.010000000000000000000000** station is at the vertex. Set flag 2 if the slave 2c. A-Key time delay input -4 Ч Initialize Solution - cos delay sin 2a_. - it)/a 201 Card 2a. sin 2c_. B-Key time Initialıza cos F input 0 H H 0 2à ч. ີ່ບ Ъ. 10 00 0404 0640 8 8 8 0 6 8 10 0504 064048 8 8 8 8 8 35 67 -31 -51 -51 -51 -51 -51 -41 1.1 4 ••• '4) '''' ••• 5 14 141 11 1 1 1

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D. Loran-C Fixing Algorithms

The development of the Loran fixing algorithms in this report is presented in more detail in a companion report [Ref. 3] and will not be repeated here.

The basic Loran-C equation [Ref. 4] can be written as

$$\mathbf{T} = [\mathbf{T}_{S} + p(\mathbf{T}_{S})] - [\mathbf{T}_{M} + p(\mathbf{T}_{M})] + [\mathbf{T}_{B} + p(\mathbf{T}_{N})] + \delta \qquad (1)$$

where

- T is the "indicated time difference" in microseconds, T_M, T_S is the distance, in microseconds, from the master and the slave to the receiver, respectively,
 - T_B is the distance, in microseconds, between the master and the slave,
 - δ is the assigned coding delay, in microseconds, and
- p(T) is the secondary phase correction, in microseconds, for an all sea water path of length T.

The quantity

$$h t = [T_B + p(T_B)] + \delta$$

is a constant for each master/slave pair. The following World Geodetic System 1972 (WGS 72) values have been adopted for Loran-C navigation [Ref. 4]:

- n = 1.000338 is the index of refraction of the surface of the earth for standard atmosphere and 100kHz electromagentic waves,
- a_e = 6378135.00 meters is the equatorial radius of the earth, and
- f = 1/298.26 is the flattening factor (1 b/a_e , where b is the polar radius) of the earth.

Accurate formulas for computing the secondary phase correction p(T) are contained in Reference 4, but for use with the handheld calculator the following linear approximation [Ref. 3] will be used:

$$p(T) = a_1 + a_2 T$$
,

where

and

$$a_1 = -0.321,$$

 $a_2 = 0.000635.$

Using this approximation, it is possible to solve Equation 1 for the quantity $T_S - T_M$. We find

$$T_{S} - T_{M} = (T - \Delta t) / (1 + a_{2})$$
 (2)

On the surface of a sphere a hyperbolic line of position can be represented by the equation [Ref. 3, page 175]

$$\tan r = \frac{\cos 2a - \cos 2c}{\sin 2c \cos \omega + \zeta \sin 2a}$$
(3)

where the origin of the coordinate system is at the prime focus of the spherical hyperbola, 2c is the spherical arc joining the foci, 2a is a constant for any one LOP, and r and ω are the spherical coordinates of a point on the LOP. If the base line of the coordinate system is the arc joining the foci then ω is the spherical polar angle from the base line to a point P on the LOP and r is the spherical polar distance (or arc) from the prime focus to P. Using the Loran system we take $\zeta = +1$ if the prime focus is at a master station and we take $\zeta = -1$ if the prime focus is at a slave station.

If we take $v = v_0/\eta$ to be the velocity of 100kHz electromagnetic radiation of the earth's surface then

$$2a = v(T_S - T_M)/a_e$$
,

or, using Eq. (2),

 $2a = (T - \Delta t)/a_{p}$, (4)

where

$$a_p = \frac{a_e(1 + a_2)}{v_0/\eta} = 21295.87 \ \mu s$$
.

The baseline between master and slave can be obtained from

$$2c = v T_{B}/a_{e} .$$
 (5)

Here 2c is computed by program card 1 (preparation of master data cards) using the algorithm in Section E.

Consider a Loran-C triplet with master stations colocated. Let ξ_1 and ξ_2 denote the azimuth angles of slave 1 (S₁) and slave 2 (S₂), respectively, measured from North toward the East from the master stations (M) (see Fig. 3). Further, let α and r denote the azimuth and spherical polar arc (distance) of the receiver (R) from M. For this geometry, Eq. (3) can be written as

$$\tan r_{i} = \frac{B_{i}}{C_{i} \cos(\alpha - \xi_{i}) + A_{i}}$$
(6)

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where

$$A_{i} = \zeta_{i} \sin 2a_{i}$$
$$B_{i} = \cos 2a_{i} - \cos 2c_{i}$$
$$C_{i} = \sin 2c_{i}$$

and

for the $i\frac{th}{t}$ Loran pair, i = 1,2. Since $r = r_1 = r_2$, tan r_i can be eliminated in Eq. (6). The resulting equation can be rewritten as

$$C \cos \alpha + S \sin \alpha = K$$
, (7)

where

$$C = B_{1}C_{2} \cos \xi_{2} - B_{2}C_{1} \cos \xi_{1},$$

$$S = B_{1}C_{2} \sin \xi_{2} - B_{2}C_{1} \sin \xi_{1},$$

$$\kappa = B_{2}A_{1} - B_{1}A_{2}.$$

and





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If we define $\rho > 0$ and γ by the equations

 $\rho \cos \gamma = C$,

and

 $\rho \sin \gamma = S,$

then

$$\rho = \sqrt{c^2 + s^2}$$

(8)

and

$$\gamma = qatn(S,C)$$

Here the function qatn(y,x) is the arctangent of y/xadjusted for the proper quadrant according to the signs of xand y. A compact form of this function is

$$qatn(y,x) = tan^{-1} \frac{y}{x + 10^{-9}t(x = 0?)} + \pi t(x < 0?)$$

where

$$t(z) = 1$$
 when z is true

and

t(z) = 0 when z is false.

When convenient we will use the notation qatn(y/x) interchangeably with qatn(y,x). The qatn function is equivalent to the polar angle obtained using the rectangular to polar conversion function on the HP-67/97.

Now substitute Eq. (8) into Eq. (7) and solve for

$$\alpha = \gamma \pm \cos^{-1}(\kappa/\rho) \tag{9}$$

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to obtain the azimuth angle α of the two points of intersection of the LOP's. Finally we obtain a value for r by substituting each α into Eq. (5). We find that

$$r = qatn \left[\frac{B_i}{C_i \cos(\alpha - \xi_i) + A_i} \right] \quad for \quad i = 1 \text{ or } 2.$$

The distance and azimuth from M or the triplet vertex can be converted into the latitude and longitude of the two possible positions of R.

The fixing algorithm then uses α and r in the direct solution algorithm of spheroidal geodesy (Section F).

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E. The Reverse (Inverse) Solution Algorithm

This *reverse* solution algorithm is a modification of the first order in flattening (f) algorithm given by Thomas [Ref. 5, pp. 8-10]. Thomas' notation has been followed as closely as possible for ease of comparison of the algorithms. The gatn function is defined in Section D. West longitudes (λ) and South latitudes (ψ) are negative. We are given the points $P_1(:_1, \lambda_1), P_2(\phi_2, \lambda_2)$ on the spheroid and are to find the distance S between the points and the forward and back azimuths, α_{12} and α_{21} . Given quantities are $\phi_1, \lambda_1, \phi_2$ and β_2 . No assumptions about the relative location of P_1 and P_2 are required. The modified *reverse* solution algorithm is:

$$\begin{split} & \gamma_{1} = \tan^{-1} [(1-f) \tan \phi_{1}], \quad i = 1, 2, \\ & \gamma_{m} = (\gamma_{1} + \gamma_{2})/2, \quad \Delta v_{m} = (\theta_{2} - v_{1})/2, \quad \Delta \lambda = \lambda_{2} - \lambda_{1}, \\ & \gamma_{m} = 2\lambda/2, \quad H = \cos^{2} \Delta v_{m} - \sin^{2} \theta_{m} = \cos^{2} \gamma_{m} - \sin^{2} \Delta \theta_{m} = \cos \theta_{1} \cos \theta_{2}, \\ & L = \sin^{2} 2\theta_{m} + H \sin^{2} \Delta \lambda_{m} = \sin^{2} (d/2), \quad 1 - L = \cos^{2} (d/2), \\ & d = \cos^{-1} (1 - 2L), \quad U = 2 \sin^{2} \theta_{m} \cos^{2} 2\theta_{m}/(1 - L), \\ & V = 2 \sin^{2} \Delta \theta_{m} \cos^{2} \gamma_{m}/L, \quad X = U + V, \quad Y = U - V, \\ & L = \sin^{2} \Delta \theta_{m} \cos^{2} \gamma_{m}/L, \quad X = U + V, \quad Y = U - V, \\ & L = \sin^{2} (\Delta \theta_{m} - S_{1})/2 = f(TX - Y)/4, \quad S = a_{e}(T - \delta_{1}d) \sin d, \\ & F = 2(Y - (1 - 2L)(4 - X)), \quad G = fT/2, \\ & = 1Fx \tan^{-1} U/2 + (1 - 2L)(4 - X)], \quad G = fT/2, \end{split}$$

 $t_{1} = qatn(-\sin \Delta \theta_{m} \cos \Delta \lambda_{m}^{*}, \cos \theta_{m} \sin \Delta \lambda_{m}^{*}),$ $t_{2} = qatn(\cos \Delta \theta_{m} \cos \Delta \lambda_{m}^{*}, \sin \theta_{m} \sin \Delta \lambda_{m}^{*}),$ $\alpha_{12} = t_{1} + t_{2}, \quad \alpha_{21} = t_{1} - t_{2}.$

This reverse solution algorithm is used by program card 1 (preparation of master data cards) to compute the baseline distance 2c and the azimuths $\xi_{\rm MS}$ and $\xi_{\rm SM}$ between the master and slave stations of a Loran pair.

Details of the modifications made to Thomas' algorithm are contained in Reference 3.

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F. The Direct Solution Algorithm

This direct solution algorithm is a modification of the first order in flattening (f) algorithm given by Thomas [Ref. 5, pp. 7-8]. Thomas' notation has been followed as closely as possible for ease of comparison of the algorithms. The qatn function is defined in Section D. West longitudes and South latitudes are negative. We are given the point $P_1(\phi_1,\lambda_1)$ on the spherioid, where ϕ_1, λ_1 are the geodetic latitude and longtiude (geographic coordinates); the forward azimuth α_{12} and the distance S to a second point $P_2(\phi_2,\lambda_2)$; and from these we are to find the geographic coordinates ϕ_2, λ_2 and the back azimuth α_{21} . The given quantities are $\frac{1}{1}, \lambda_1, \alpha_{12}$ and S. No assumptions about the relative location of P_1 and P_2 are required. The modified direct solution algorithm is:

$$\begin{split} \theta_1 &= \tan^{-1} \{ (1-f) \ \tan \ \phi_1 \}, \qquad \mathsf{M} = \cos \ \theta_1 \ \sin \ \alpha_{12} \\ \mathsf{N} &= \cos \ \theta_1 \ \cos \ \alpha_{12}, \quad c_1 &= f\mathsf{M}, \quad c_2 &= f(1-\mathsf{M}^2)/4, \\ \mathsf{D} &= 1 - 2c_2 - c_1\mathsf{M}, \qquad \mathsf{P} = c_2/\mathsf{D}, \qquad \theta_1 &= \operatorname{qatn}(\mathsf{N}, \ \sin \ \theta_1) \\ \mathsf{d} &= \mathsf{S}/(\mathsf{a}_e^{\mathsf{D}}), \qquad \mathsf{u} = 2(\sigma_1^{-}\mathsf{d}), \qquad \mathsf{W} = 1 - 2\mathsf{P} \ \mathsf{cos} \ \mathsf{u}, \\ \mathsf{V} &= \cos(\mathsf{u} + \mathsf{d}), \qquad \mathsf{Y} = 2\mathsf{P}\mathsf{V}\mathsf{W} \ \mathsf{sin} \ \mathsf{d}, \qquad \Delta \sigma = \mathsf{d}-\mathsf{Y}, \\ \theta_2 &= \operatorname{qatn}\{-\mathsf{M}, -(\mathsf{N} \ \cos \ \Delta \sigma - \sin \ \theta_1 \ \sin \ \Delta \sigma)\}, \\ \mathsf{K} &= (1-f)\{\mathsf{M}^2 + (\mathsf{N} \ \cos \ \Delta \sigma - \sin \ \theta_1 \ \sin \ \Delta \sigma)^2\}^{1/2}, \\ \theta_3 &= \tan^{-1}\{(\sin \ \theta_1 \ \cos \ \Delta \sigma + \mathsf{N} \ \sin \ \Delta \sigma)/\mathsf{K}\}, \\ \theta_4 &= \operatorname{qatn}(\sin \ \beta^* \ \sin \ \alpha_{12}, \ \cos \ \theta_1 \ \cos \ \Delta \sigma - \sin \ \theta_1 \ \sin \ \Delta \sigma \ \cos \ \alpha_{12}) \\ \mathsf{H} &= \phi_1^{+1}, \qquad \theta_4 &= (\mathsf{N} - \mathsf{H}, \qquad \theta_2 = \mathsf{N}_1 + \mathsf{A}), \\ \mathbf{32} &= \mathsf{A}\mathsf{L} \end{split}$$

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This direct solution algorithm is used by program card 3 (improved fix program) to compute the latitude and longitude of the receiver using the azimuth and range of the receiver from the Loran triplet vertex.

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Details of the modifications made to Thomas' algorithm are contained in Reference 3.

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G. Discussion and Some Typical Results

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The HP-67 program design specifications of COMPATWINGSPAC [Ref. 6] are contained in the following statement.

> "There is a need for an HP-67 program that will compute a geographical position from two Loran delay rate readings. Several methodologies are available to compute the desired position but computational complexities increase with the desired accuracy and flexibility. The most desirable accuracy would be an error of less than 4 n.m. at a range of 500 n.mi. with less error closer to the stations. It is likely that program length considerations will require that the station pairs have a common site (i.e. two slaves or two masters at the same location). This is not an unusual situation as evidenced by strings of station pairs along coast lines. A data card will probably be necessary for the station pairs to be used. However, more than one program card is unacceptable due to the decrease in functional utility when compared to the manual plotting method. As a final requirement, the fix should be obtainable on either side of the baselines connecting the stations, and not limited to a geometric position relative to one side or the other of the stations."

It was further stated that the maximum computation time to obtain a fix be 1.5 minutes.

It is felt that these design goals have been satisfied. Although one program is required to prepare master data cards for all Loran-C pairs and a second card is required to prepare

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operational data cards, one each for every triplet, this preparation should be done only once. The data cards should be supplied to users verified and labeled, by the Fleet Mission Program Library. One program card and an appropriate operational data card are all that is required for the fixing algorithm.

The fixing algorithm will display one of the two possible receiver positions in 38 seconds following the entry of the time delay readings. Since there are situations in which *either* of the two solutions could be the valid solution; the decision of which solution to use should be left to the operator, not the program designer.

Testing of the algorithm for all Loran-C triplets and positions relative to those triplets was too extensive a program to be carried out in the available time. Some "typical" scenarios however are presented in Tables I through IV. As can be seen all errors are all well within the design specifications of 4 n.mi at 500 n.mi range from the stations. The time delay values in these Tables were generated using a program discussed in Reference 3. It is recommended that the P-3 community test the algorithm for accuracy in known areas of operation and examine the results for possible regions in which the algorithm may fall outside the design requirements. Such testing should be compatible with the known "unreliable regions" shown on the Loran-C charts.

Posi	tion	Indicated	Time Delay	<u> </u>	Fix	
Lat	Long	9940X	9940¥	Lat(N)	Long(W)	Error n.mi
24°N	122°W	27726.19	40912.76	23°59'55"	122°00'01"	0.08
26	122	27715.97	40998.39	25°59'57"	122°00'01"	0.05
28	122	27702.41	41117.84	27°59'59"	122°00'00"	0.02
30	122	27683.53	41291.85	29°59'59"	122°00'00"	0.02
32	122	27655.47	41555.46	32°00'00"	122"00'00"	0.00
34	122	27609.63	41959.57	34°00'00"	122°00'00"	0.00
36	122	27523.56	42544.11	36°00'00"	121°59'59"	0.01
38	122	27334.61	43248.22	38°00'00"	121°59'58"	0.03

Table I. Moffett Field South

Table II. Moffett Field West

Posi	tion	Indicated	Time Delay		Fix	
Lat	Long	9940Y	9940w	Lat(N)	Long(W)	Error n.mi
37°N	122°W	42892.86	16257.23	36°59'59"	122°00'01"	0.02
37	125	43056.68	15765.13	37°00'00"	125°00'00"	0.00
37	128	43137.78	15327.12	37°00'00"	128°00'00"	0.00
37	131	43191.10	14970.77	37°00'00"	131°00'00"	0.00
37	134	43232.38	14683.74	37°00'00"	134°00'00"	0.00
37	137	43267 .42	14449.40	37°00'00"	137°00'00"	0.00
37	140	43298.80	14254.02	37°00'00"	140°00'01"	0.01
37	143	43327.85	14087.43	37°00'01"	142°59'59"	0.02

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Posi	tion	Indicated	Time Delay		Fix	
Lat	Long	7930 Z	9930x	Lat(N)	Long (W)	n.mi
60°N	30°W	52437.86	28451.72	60°00'03"	29°59' 32"	0.24
58	35	51960.93	28391.50	58°00'00"	34°59'46"	0.11
56	40	50992.37	28359.15	55°59'59"	39°59'54"	0.06
54	45	49292.46	28370.85	53°59'59"	44°59'57"	0.03
52	50	47165.60	28490.64	52°00'00"	49°59'59"	0.01
50	55	45236.59	29070.48	50°00'00"	55°00'00"	0.00
48	60	44505.60	30991.94	48°00'00"	60°00'00"	0.00
46	65	44475.70	33697.14	46°00'00"	65°00'00"	0.00
44	70	44588.91	36567.42	43°59'59"	69 ° 59'59"	0.02

Table III. Brunswick Northeast

Table IV. Jacksonville Southeast

Posit	ion	Indicated	Time Delay		Fix	
Lat	Long	9930W	9930X	Lat(N)	Long(W)	Error n.mi
9°N	47°W	13058.04	36466.46	8°59'19"	46°59'22"	0.92
12	52	12984.71	37288.35	11°59'34"	51°59'37"	0.57
15	57	12898.73	38267.58	14°59'44"	56°59'47"	0.34
18	62	12793.91	39431.32	17°59'52"	61°59'54"	0.16
21	67	12656.52	40794.36	20°59'56"	66°59'57"	0.08
24	72	12451.30	42330.55	23°59'59"	71°59'59"	0.02
27	77	12097.12	43876.62	27°00'01"	77°00'00"	0.02
30	82	12973.95	44768.53	30°00'01"	82°00'06"	0.09

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H. References

- J. A. Pierce, A. A. McKenzie, and R. H. Woodward, editors, LORAN, M.I.T. Radiation Laboratory Series, McGraw-Hill Book Company, Inc., 1948.
- G. Hefley, The Development of Loran-C Navigation and Timing, National Bureau of Standards Monograph 129, U. S. Department of Commerce, U. S. Government Printing Office, Washington, D.C. 20402, October 1972.
- 3. R. H. Shudde, "An Algorithm for Position Determination Using Loran-C Triplets with a BASIC Program for the Commodore 2001 Microcomputer," Technical Report NPS55-80-009, March 1980, Naval Postgraduate School, Monterey, CA 93940.
- 4. LORAN HYPERBOLIC LOP FORMULAS AND GENERAL SPECIFICATIONS FOR LORAN-C (20 June 1949) were obtained from G. R. Young, Acting Chief, Navigation Department, Defense Mapping Agency, Hydrographic/Topographic Center, Washington, D.C. by private communication, 5 March 1980.
- Paul D. Thomas, "Spheroidal Geodesics, Reference Systems, and Local Geometry," SP-138, U. S. Naval Oceanographic Office, Washington, D.C., January 1970.
- Private communication from COMPATWINGSPAC representatives, Moffett Field, CA., October 1979.

APPENDIX. Loran-C Station Parameters

The following list contains the pertinent parameters for each Loran-C station pair. This list was compiled from data in Reference 4. Each column contains the following information:

- 1. The Loran-C station pair designator
- At, the sum of the coding delay plus one way baseline time, including the secondary phase correction for an all seawater path, in microseconds.
- 3. The master station latitude.
- 4. The master station longitude.
- 5. The slave station latitude.
- 6. The slave station longitude.

In this list, negative longitudes are West and positive longitudes are East. If desired, this convention may be reversed since the algorithms are independent of such external conventions; if this is done, care should be taken that the signs of all longitudes in the list are reversed. In columns 3 through 6 the latitudes and longitudes appear to be in decimal form, but the actual format is DDD.MMSSFF (which is compatible with the HP-67/97 H.MS input mode) where

> DDD designates degrees, MM designates minutes, SS designates seconds, and FF designates hundredths of seconds.

4990X.	15972.	23,	16.	444395,	-169.	303120.	20.	144916,	-155.	530970
4990Y/	34253.	18,	16.	444395,	-169.	303120.	,28.	234177/	-178.	173020
5930X/	13131.	.88,	46.	.482720,	-067.	553771.	,41.	151193,	-069.	583909
5930Y)	28755.	.02,	46.	482720,	-067.	553771,	46.	463218,	-053.	102816
5990X.	13343.	.60,	51.	575878,	-122.	220224.	, 55,	262085/	-131.	151965
5990Y,	28927.	.36,	51.	575878.	-122.	220224.	47.	0347997	-119.	443953
5990Z,	42266.	63,	51.	575878,	-122.	220224.	50.	362972,	-127.	212935
7930W)	15068.	.02,	59.	591727,	-045.	102747.	,64.	542658.	-023.	552175
7930X,	27803.	.77,	59.	591727,	-045.	102747.	,62.	175968.	-007.	042671
7930Z.	48212.	20,	59.	591727,	-045.	102747.	. 46.	463218.	-053.	102816
7960X.	13804.	.45.	63.	194281,	-142.	483190.	, <u>57</u> ,	262021.	-152.	221122
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-7970M	30065.	64,	62.	175968,	-007.	.042671.	-54.	482980.	+008.	173633
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Coverage of Loran-C Systems

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Station	Location
4990	Central Pacific
5930	East Coast, Canada
5990	West Coast, Canada
7930	North Atlantic
7960	Gulf of Alaska
7970	Norwegian Sea
7980	Southeast U.S.A.
7990	Mediterranean Sea
8970	Great Lakes
9930	East Coast, U.S.A.
9940	West Coast, U.S.A.
9960	Northeast U.S.A.
9970	Northwest Pacific
9990	North Pacific

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